

TODAY'S AGENDA: Week of May 10- May 18

- Work on Khan Academy Mission:
- Whole Class Lessons

- Today's Objective:

- Parallel and Perpendicular Lines

- Standards:
- G.GPE. B.5:
- On the coordinate plane:
 - > a) Explore the proof for the relationship between slopes of parallel and perpendicular lines;
 - > b) Determine if lines are parallel, perpendicular, or neither, based on their slopes; and
 - > c) Apply properties of parallel and perpendicular lines to solve geometric problems.

Parallel and Perpendicular Lines from a Graph

- Parallel lines go on forever in two directions and never intersect.
- Parallel lines have the **SAME SLOPE**
- Perpendicular lines intersect at a right angle.
- Perpendicular lines have **NEGATIVE RECIPROCAL SLOPES**

SLOPE

$$m = \frac{y_2 - y_1}{x_2 - x_1}$$

$(3, 4)$ $(-4, 7)$
 x_1, y_1 x_2, y_2

$\frac{7 - 4}{-4 - 3} = \frac{3}{-7}$

Some
 $\frac{3}{-7}$

NEGATIVE RECIPROCAL SLOPES

change sign

flipped

$$\frac{7}{3}$$

perpendicular lines have neg. rec. slopes

neg. rec.

Are the lines in the figure parallel, perpendicular, or neither?

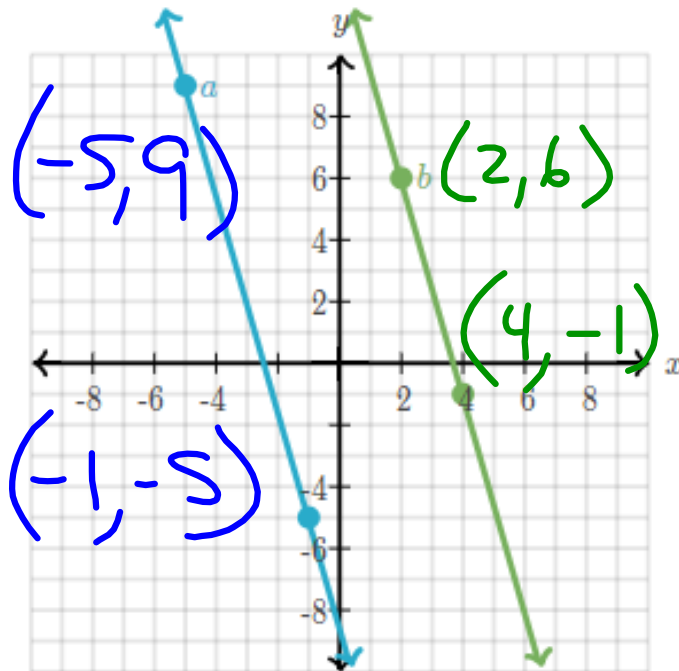
Choose 1 answer:

Parallel

Perpendicular

Neither

$$m = \frac{y_2 - y_1}{x_2 - x_1} = \frac{-5 - 9}{-1 + 5} = \frac{-14}{4} = -\frac{7}{2}$$



$$m = \frac{-1 - 6}{4 - 2} = \frac{-7}{2}$$

perpendicular: $\frac{2}{7}$

One line passes through the points (2, 1) and (5, 7). Another line passes through points (-3, 8) and (8, 3).

Are the lines parallel, perpendicular, or neither?

Choose 1 answer:

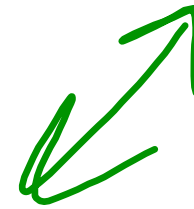
(A) Parallel

(B) Perpendicular

(C) Neither

$$\frac{7-1}{5-2} = \frac{6}{3} = 2$$

$$\frac{3-8}{8+3} = \frac{-5}{11}$$



$$\begin{array}{cc} (-7, 5) & (-1, -3) \\ x_1, y_1 & x_2, y_2 \end{array}$$

$$m = \frac{y_2 - y_1}{x_2 - x_1} = \frac{-3 - 5}{-1 + 7} = \frac{-8}{6} = \frac{-4}{3}$$

perpendicular
I
4/3

One line passes through the points $(1, 9)$ and $(4, -9)$. Another line passes through points $(6, 5)$ and $(8, -5)$.

Are the lines parallel, perpendicular, or neither?

Choose 1 answer:

A Parallel

B Perpendicular

C Neither

Parallel and Perpendicular Lines from Equations

Slope

y-intercept

$$y = mx + b$$

Same = parallel

negative reciprocal = perpendicular

What do the following two equations represent?

$$-x - 3y = -1$$

$$-x - 3y = -1$$

$$-x - 3y = -1$$

$$-x - 3y = -1$$

Choose 1 answer:



Equal lines



Parallel lines



Perpendicular lines



None of the above

What do the following two equations represent?

$-4x - 5y = -4$

$-4x - 5y = -4$ (with $-4x - 5y$ circled in blue and an arrow pointing to the right)

$4x + 5y = 4$

$4x + 5y = 4$ (with $4x + 5y$ circled in green and an arrow pointing to the right)

$4x + 5y = 4$

Choose 1 answer:

$-5y = 4x - 4$ (with $-5y$ circled in red and -5 crossed out in red)

$5y = -4x + 4$ (with $5y$ circled in green and 5 crossed out in red)

Equal lines

Parallel lines
Same

Perpendicular lines

None of the above

$y = -\frac{4}{5}x + \frac{4}{5}$ (with $-\frac{4}{5}$ circled in green)

$y = -\frac{4}{5}x + \frac{4}{5}$ (with $-\frac{4}{5}$ circled in green)

$5y = 4x$

What do the following two equations represent?

$$-4x + 3y = 5$$

$$-9x - 12y = -1$$

Choose 1 answer:

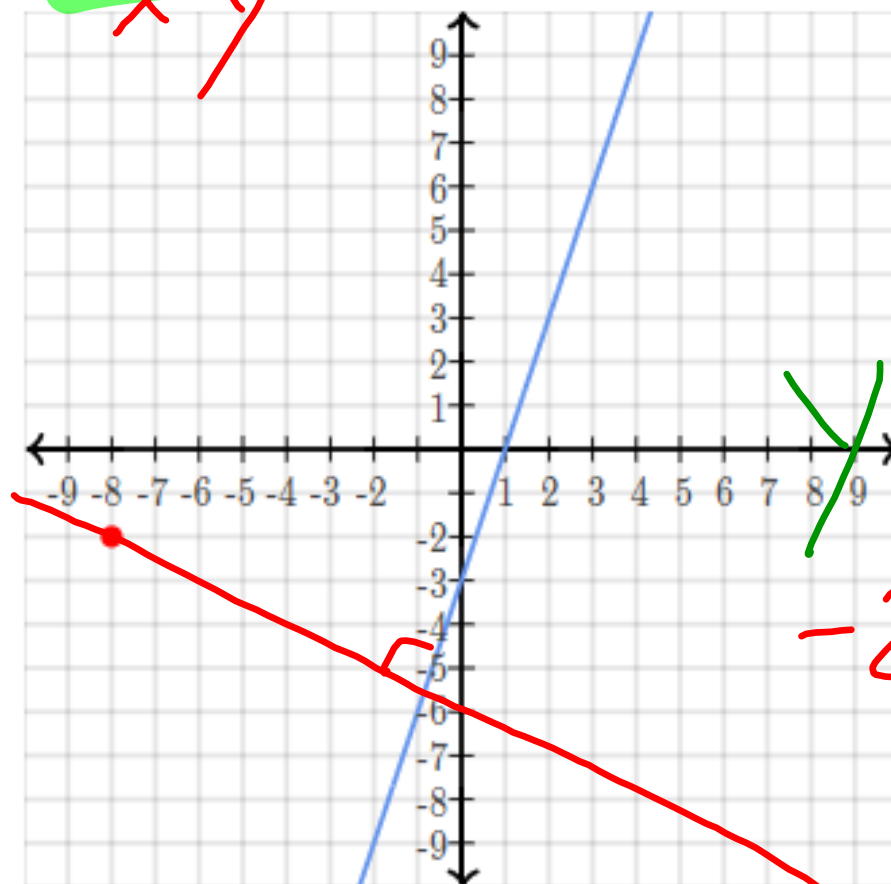
A Equal lines

B Parallel lines

C Perpendicular lines

D None of the above

Find the slope and y-intercept of the line that is perpendicular to $y = 3x - 3$ and passes through the point $(-8, -2)$.



$$m = \boxed{-\frac{1}{3}}$$

$$b = \boxed{-\frac{14}{3}}$$

$$y = 3x - 3$$

$$y = -\frac{1}{3}x + b$$

$$-2 = -\frac{1}{3}(-8) + b$$

$$-2 = \frac{8}{3} + b = -\frac{14}{3}$$

$-\frac{8}{3}$ ←

$$\underline{-2x - 4y = -3}$$

$$\begin{array}{r} -4y = +2x - 3 \\ \hline -4 \quad -4 \end{array}$$

$$y = -\frac{1}{2}x + \frac{3}{4}$$

$$\underline{6x + 12y = 9}$$

$$\begin{array}{r} 12y = -6x + 9 \\ \hline 12 \end{array}$$

$$y = -\frac{1}{2}x + \frac{9}{12} = \frac{3}{4}$$

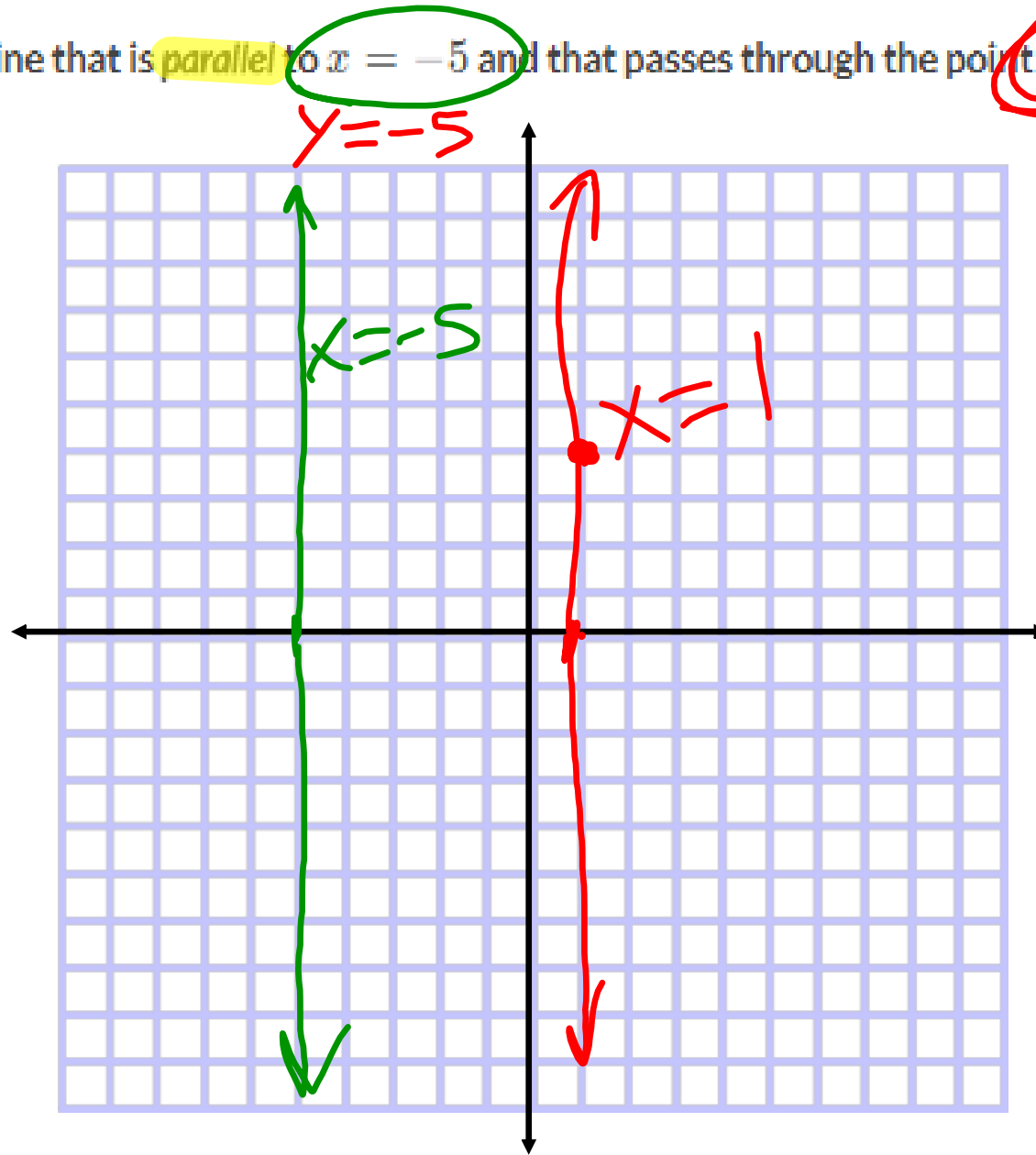
Equal!!

Writing Equations of Parallel and Perpendicular Lines

Your answer will ALWAYS^{*} be in the form:

$$y = mx + b$$

Write the equation of a line that is parallel to $x = -5$ and that passes through the point $(1, 4)$.



Write the equation of a line that is perpendicular to $y = 5$ and that passes through the point $(-7, -5)$.

$$x = -7$$

parallel (same letter)

perpendicular (opposite letter)

Write the equation of a line that is parallel to $y = 0.6x + 3$ and that passes through the point $(-3, -5)$.

same \swarrow $y = 0.6x + 3$ $(-3, -5)$
 slope \swarrow x y

$y = 0.6x + b$ \swarrow plug-in
 $-5 = 0.6(-3) + b$
 $-5 = -1.8 + b$
 $+1.8 \quad +1.8$

$-3.2 = b$ $y = 0.6x - 3.2$

Skills You Should Be Working on:

1. Parallel and Perpendicular lines from graph
2. Parallel and Perpendicular lines from equation
3. Write equations of parallel and perpendicular lines